# New Heights Charter School of Brockton Algebra I Packet

March/April 2020

March 2020

Dear New Heights Charter School Scholars,

Thank you for taking time to complete this Algebra I packet. It is important to refine skills in academic areas during periods of absence from school. Scholars should work through this packet and complete as much work as possible. A reference sheet is located at the end of the packet, and a reference sheet is available as an attachment.

Submit this completed packet to your math teacher. As a reminder, the work completed in this packet will not count towards your grades, and it is considered academic enrichment.

Sincerely,

Ms. Miceli Director of Curriculum

# **Proportions**

## Write and solve a proportion to answer each problem. Show your work.

1.	Tommy types 54 words per minute, with an average of 3 mistakes. How many mistakes
	would you expect Tommy to make if he typed 300 words?

2. Jackie burns 250 calories per hour doing aerobics. She has to burn 3500 calories to lose one pound. How long will Jackie have to work out to lose 5 pounds?

#### Percent

The items below were purchased in a city with a sales tax rate of 5%. Find the amount of sales tax on each purchase.

- 1. A DVD for \$18.00
- 2. A computer hard drive for \$140.00
- 3. A bathing suit for \$65.00
- 4. A bicycle for \$150.00

## **Table of Values**

Plot each point in the table on a coordinate grid. Identify the <u>rate of change</u> for each.

1.

X	-3	-2	-1	0	1	2	3
Y	15	13	11	9	7	5	3

For each equation, create a table of values and plot the points. Identify the rate of change.

2. y = x + 4

Х	-2	-1	0	1	2
у					

3. y = 2x - 6

X	Y
-2	
-1	
0	
1	
2	

# **Adding and Subtracting Integers**

Simplify each expression

**1.** 
$$-2 + (-3)$$
 **2.**  $8 - 7 + 4$  **3.**  $8 + (-5)$ 

2. 
$$8 - 7 + 4$$

3. 
$$8 + (-5)$$

4. 
$$15 + (-3)$$

5. 
$$-16 + 8$$

**4.** 
$$15 + (-3)$$
 **5.**  $-16 + 8$  **6.**  $7 + (-10)$ 

**7.** 
$$-9 + (-5)$$
 **8.**  $-12 + 14$  **9.**  $8 + 7$ 

8. 
$$-12 + 14$$

9. 
$$8 + 7$$

**10.** 
$$-63 - 89$$

13. 
$$72 - 15$$

**15.** 
$$17 - (-46)$$

16 
$$-78 - (-53)$$

17 
$$-19 - (-12)$$

# **Order of Operations - Integers**

#### Accentuate the Negative

Find the value of each expression.

1. 
$$(8+2) \times 9$$

**2.** 
$$5 - 1 \div 4$$

**1.** 
$$(8+2) \times 9$$
 **2.**  $5-1 \div 4$  **3.**  $(6+3) \div 18$  **4.**  $80-6 \times 7$ 

**4.** 
$$80 - 6 \times 7$$

**5.** 
$$4 \times 6 + 3$$

6. 
$$4 \times (6 + 3)$$

**5.** 
$$4 \times 6 + 3$$
 **6.**  $4 \times (6 + 3)$  **7.**  $35 - 6 \times 5$  **8.**  $8 \div 3 + 6$ 

8. 
$$8 \div 3 + 6$$

**9.** 
$$(-4)^2 + 10 \cdot 2$$
 **10.**  $-4^2 + 10 \cdot 2$  **11.**  $(5 \cdot 3)^2 + 8$ 

**10.** 
$$-4^2 + 10 \cdot 2$$

**11.** 
$$(5 \cdot 3)^2 + 8$$

**12.** 
$$5 \cdot 3^2 + 8$$

**12.** 
$$5 \cdot 3^2 + 8$$
 **13.**  $9 + (7 - 4)^2$  **14.**  $-9 + 7 - 4^2$ 

**14.** 
$$-9 + 7 - 4^2$$

**15.** 
$$(-6)^2 + 3^3 - 7$$

**16.** 
$$-6^2 + 3^3 - 7$$

**15.** 
$$(-6)^2 + 3^3 - 7$$
 **16.**  $-6^2 + 3^3 - 7$  **17.**  $2^3 + (8 - 5) \cdot 4 - 5^2$ 

**18.** 
$$(2^3 + 8) - 5 \cdot 4 - 5^2$$
 **19.**  $2^3 \cdot 3 - 5 \cdot 5^2 + 8$  **20.**  $2^3 \cdot 3 - 5(5^2 + 8)$ 

**19.** 
$$2^3 \cdot 3 - 5 \cdot 5^2 + 8$$

**20.** 
$$2^3 \cdot 3 - 5(5^2 + 8)$$

# **Multiplying and Dividing Rational Numbers**

#### Accentuate the Negative

Use the algorithms you developed to find each value.

1. 
$$-\frac{1}{6} \cdot 2\frac{3}{4}$$

**2.** 
$$\frac{3}{16} \div \left(-\frac{1}{8}\right)$$
 **3.**  $-\frac{31}{56} \cdot (-8)$ 

3. 
$$-\frac{31}{56} \cdot (-8)$$

4. 
$$-5\frac{7}{12} \div 12$$

5. 
$$-8 \div \frac{1}{4}$$

**4.** 
$$-5\frac{7}{12} \div 12$$
 **5.**  $-8 \div \frac{1}{4}$  **6.**  $-3\frac{1}{6} \div \left(-2\frac{1}{12}\right)$ 

7. 
$$8\frac{3}{4} \cdot 3\frac{7}{8}$$

8. 
$$-\frac{11}{12} \div \frac{5}{6}$$

**8.** 
$$-\frac{11}{12} \div \frac{5}{6}$$
 **9.**  $4\frac{9}{28} \cdot (-7)$ 

**10.** 
$$-1\frac{1}{15} \div 15$$

11. 
$$-3 \div \frac{3}{4}$$

**10.** 
$$-1\frac{1}{15} \div 15$$
 **11.**  $-3 \div \frac{3}{4}$  **12.**  $-2\frac{7}{8} \div 3\frac{3}{4}$ 

**13.** 
$$-\frac{23}{24} \cdot (-8)$$
 **14.**  $\frac{7}{8} \cdot \left(-\frac{2}{7}\right)$  **15.**  $-7 \div \frac{1}{9}$ 

**14.** 
$$\frac{7}{8} \cdot \left(-\frac{2}{7}\right)$$

**15.** 
$$-7 \div \frac{1}{9}$$

# **Adding and Subtracting Rational Numbers**

Accentuate the Negative

Find each sum or difference as a mixed number or fraction in simplest form.

1. 
$$\frac{3}{4} + \frac{7}{8}$$

**2.** 
$$-1\frac{1}{6} + 2\frac{2}{3}$$
 **3.**  $4\frac{1}{2} - 7\frac{7}{8}$ 

3. 
$$4\frac{1}{2} - 7\frac{7}{8}$$

**4.** 
$$-3\frac{5}{6} - \left(4\frac{1}{12}\right)$$
 **5.**  $\frac{5}{18} + \frac{7}{12}$  **6.**  $-4\frac{7}{20} + 3\frac{9}{10}$ 

5. 
$$\frac{5}{18} + \frac{7}{12}$$

**6.** 
$$-4\frac{7}{20} + 3\frac{9}{10}$$

**7.** 
$$5\frac{8}{21} - \left(-3\frac{1}{7}\right)$$
 **8.**  $1\frac{19}{24} + 2\frac{23}{20}$  **9.**  $3\frac{16}{25} - 4\frac{7}{20}$ 

**8.** 
$$1\frac{19}{24} + 2\frac{23}{20}$$

9. 
$$3\frac{16}{25} - 4\frac{7}{20}$$

Write each answer as a fraction or mixed number in simplest form.

**10.** 
$$14.6 + \left(-3\frac{1}{5}\right)$$

**11.** 
$$-7\frac{3}{4} + 4.125$$

**11.** 
$$-7\frac{3}{4} + 4.125$$
 **12.**  $5.75 + \left(-2\frac{1}{8}\right)$ 

# **Operations with Rational Numbers**

**14.** 
$$(-6)(-9)$$
 **15.**  $(-3)^4$ 

**16.** 
$$-2^5$$

17. 
$$(6)(-8)$$

**19.** 
$$2(-4)(-6)$$
 **20.**  $-30 \div (-5)$  **21.**  $\frac{-52}{-13}$ 

21. 
$$\frac{-52}{-13}$$

**22.** 
$$(-8)(5)(-3)$$
 **23.**  $-7^2$ 

23. 
$$-7^2$$

**25**. 
$$\frac{-68}{17}$$

**25.** 
$$\frac{-68}{17}$$
 **26.**  $\frac{(-4)(-13)}{-26}$ 

**27.** 
$$\frac{225}{(-3)(-5)}$$

28. 
$$2^4 - 3^2 + 5^2$$

29. 
$$(-8)^2 - 4^3$$

**28.** 
$$2^4 - 3^2 + 5^2$$
 **29.**  $(-8)^2 - 4^3$  **30.**  $32 \div (-7 + 5)^3$ 

**31.** 
$$\frac{3}{4} \div \left(-\frac{3}{7}\right)$$

**31.** 
$$\frac{3}{4} \div \left(-\frac{3}{7}\right)$$
 **32.**  $18 + 4^2 \div (-8)$  **33.**  $26 \div [4 - (-9)]$ 

#### **Fractions - Word Problems**

- 1. Suppose you have 2  $\frac{1}{2}$  oranges. If a student serving consists of  $\frac{3}{4}$  an orange, how many student servings (including parts of a serving) can you make?
- 2. Pat is also tying ribbons into bows. Pat sees the same  $7\frac{1}{2}$  feet of ribbon measured out and says "Since my bows are bigger than Carmen's, there is only enough for me to make  $2\frac{1}{4}$  bows." How much ribbon does Pat use on each bow?

### **Evaluating Expressions**

For Exercises 1–26, evaluate the expression for the given value of x.

1. 
$$3.5x - 10$$
 when  $x = 2$ 

2. 
$$45 - 2x$$
 when  $x = 6$ 

3. 
$$-3 - x$$
 when  $x = \frac{1}{2}$ 

**4.** 
$$4x + 9$$
 when  $x = 11$ 

**5.** 
$$2x^2$$
 when  $x = 8$ 

**6.** 
$$11 - 3x^2$$
 when  $x = 1$ 

7. 
$$4.5 + x^2$$
 when  $x = 1.5$ 

8. 
$$6x^2 + 13$$
 when  $x = -10$ 

**9.** 
$$6x^2 + x - 11$$
 when  $x = 2$ 

**10.** 
$$6x^2 + x - 11$$
 when  $x = -2$ 

**11.** 
$$12 - 2x^2 + 5x$$
 when  $x = -4$ 

**11.** 
$$12 - 2x^2 + 5x$$
 when  $x = -4$  **12.**  $12 - 2x^2 + 5x$  when  $x = 4$ 

**13.** 
$$x(31 - x)$$
 when  $x = 3$ 

**14.** 
$$(x + 5)(x - 1)$$
 when  $x = 0$ 

**15.** 
$$(x - 1.5)(x + 42)$$
 when  $x = 1.5$ 

**16.** 
$$(31 - x)x$$
 when  $x = -3$ 

**17.** 
$$\frac{36}{x^2}$$
 when  $x = -6$ 

**18.** 
$$\frac{x^2}{24}(x+7)$$
 when  $x=-7$ 

**19.** 
$$42(x + 1)$$
 when  $x = 4$ 

**20.** 
$$\frac{3(16-x)}{2x}$$
 when  $x = 10$ 

**21.** 
$$\frac{x}{4} + 6(x - 12)$$
 when  $x = 12$ 

**22.** 
$$7x(3 + x)$$
 when  $x = -4$ 

**23.** 
$$7x^2 - x + 10$$
 when  $x = 2$ 

**24.** 
$$8x - 2x(6 - x)$$
 when  $x = 0$ 

**25.** 
$$0.5x^2 + x - 20$$
 when  $x = 10$ 

**26.** 
$$(x + 7)(x - 2)$$
 when  $x = -5$ 

# **Distributive Property**

Say It With Symbols

Use the Distributive Property to write each expression in expanded form.

**1.** 
$$2(x + 6)$$

**2.** 
$$-5(8-b)$$

3. 
$$4(-x+7)$$

**4.** 
$$-\frac{3}{4}(12-16d)$$

**5.** 
$$\frac{2}{3}(6h-1)$$

**4.** 
$$-\frac{3}{4}(12-16d)$$
 **5.**  $\frac{2}{3}(6h-1)$  **6.**  $(-3.2x+2.1)(-6)$ 

7. 
$$3.5(3x - 8)$$

8. 
$$4(x + 7)$$

**7.** 
$$3.5(3x - 8)$$
 **8.**  $4(x + 7)$  **9.**  $-2.5(2a - 4)$ 

**10.** 
$$\frac{2}{3}(12-15d)$$

**11.** 
$$-2(k-11)$$

**10.** 
$$\frac{2}{3}(12-15d)$$
 **11.**  $-2(k-11)$  **12.**  $-\frac{1}{3}(6h+15)$ 

# **Solving Equations**

Solve each equation. Show your work and check your solution.

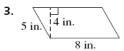
# Area Review – Show all work

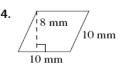
#### Filling and Wrapping

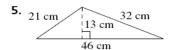
#### Find the area of each figure.

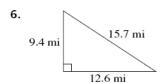


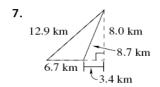


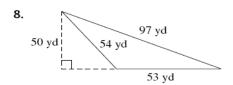


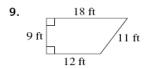


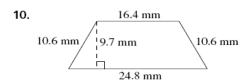






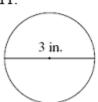


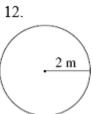




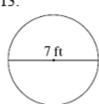
Find the **circumference** and the **area** of each circle.

11.





13.



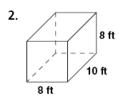
# **Surface Area and Volume**

Find the Surface Area and Volume of each rectangular prism.

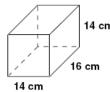
**Filling and Wrapping** 

Find the volume of each closed box.

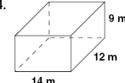




3.



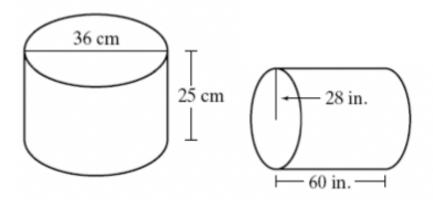
1



# **Volume of cylinders**

Find the volume of each cylinder. Write the formula and show all work.

1. 2.



- 3. A water storage tank has a cylindrical shape. The base has a diameter of 18 meters and the tank is 32 meters high. How much water, to the nearest cubic unit, can the tank hold?
- 4. A cylindrical juice container is 9 inches tall and has a radius of 2 inches. What is the volume of the container to the nearest whole unit?

# Simplify.

# **Working with Exponents**

1) 150

$$(2)(2^{-3})(3)^3$$

2) 5-2

Evaluate and write your answer in scientific notation.

5)

$$6.25 \times 10^{-4}$$

$$1.25 \times 10^2$$

(*ONLY* for students who have this accommodation listed in their IEP or 504 plan)

General Problem-Solving Strategies	Properties
<ul> <li>Reread the question for clarity</li> <li>Circle or highlight key terms</li> <li>Calculate and solve</li> <li>Circle my answer</li> <li>See if my answer makes sense</li> <li>Geometry and Measurement Abbreviations</li> <li>l = length</li> <li>w = width</li> <li>h = height</li> <li>s = length of a side</li> <li>b = length of the base</li> <li>r = radius</li> <li>d = diameter</li> <li>A = area</li> <li>B = area of the base</li> <li>P = perimeter</li> <li>C = circumference</li> <li>M = midpoint</li> </ul>	<ul> <li>a · (b + c) = a · b + a · c</li> <li>a + (b + c) = (a + b) + c</li> <li>a · (b · c) = (a · b) · c</li> <li>a + b = b + a</li> <li>a · b = b · a</li> <li>Symbols</li> <li>≤ is less than</li> <li>&gt; is greater than</li> <li>= is equal to</li> <li>  absolute value  </li> <li>≤ is less than or equal to</li> <li>≥ is greater than or equal to</li> <li>≠ is not equal to</li> <li>≠ is not equal to</li> <li>≈ is approximately equal to</li> <li>≃ is congruent to</li> <li>~ is similar to</li> <li>  is parallel to</li> <li>⊥ is perpendicular to</li> </ul>
General Formulas	Coordinate Plane
• $\pi \approx 3.14$ • $a^2 + b^2 = c^2$ • $d = rt$ $distance = rate \cdot time$ • $I = prt$ $Interest = principal \cdot rate \cdot time$ • $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	• $Ax + By = C$

Fractions	Statistics	
• $\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$ • $\frac{a}{b} - \frac{c}{d} = \frac{ad - bc}{bd}$ • $\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$ • $\frac{a}{b} \div \frac{c}{d} = \frac{ad}{bc}$	<ul> <li>me<u>A</u>n</li> <li>me<u>DI</u>an</li> <li><u>MO</u>de</li> <li><u>R</u>ang<u>E</u></li> </ul>	
Probability	Percentages and Proportions	
• $P = \frac{favorable\ outcomes}{possible\ outcomes}$	• $\frac{is}{of} = \frac{\%}{100}$ • if $\frac{a}{b} = \frac{c}{d}$ , then $ad = bc$	
Transformations	Vocabulary	
<ul> <li>tran<u>SL</u>ation</li> <li>re<u>FL</u>ection</li> <li>ro<u>T</u>ation</li> </ul>	<ul> <li>factor · factor = product</li> <li>dividend ÷ divisor = quotient</li> <li>numerator / denominator</li> </ul>	
Divisibility Rules	Angles	
2 If the last digit is even 3 If the sum of the digits can be divided by 3 5 If the last digit is 0 or 5	<ul><li>Complementary 90</li><li>Supplementary 180</li></ul>	
6 If the number is divisible by both 2	Mnemonics and Devices	
and 3  9 If the sum of the digits can be divided by 9  10 If the last digit is 0	<ul><li>PEMDAS</li><li>FOIL</li></ul>	
Num	ber Line	
<del>-5 -4 -3 -2 -1</del>	<del>                                     </del>	